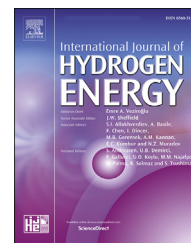


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# CFD simulation of methane steam reforming in a membrane reactor: Performance characteristics over range of operating window

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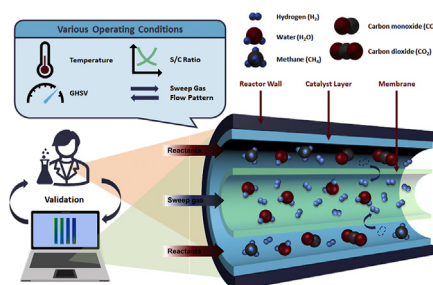
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## HIGHLIGHTS

- 3D CFD analysis of methane steam reforming in a membrane reactor.
- Xu formant based kinetic model and Sieverts' law-based permeation model were coupled.
- The CFD model evaluates the temperature, GHSV, S/C ratio and sweep gas flow pattern.
- Key performance phenomena were identified, and optimum conditions were suggested.

## GRAPHICAL ABSTRACT



## ARTICLE INFO

### Article history:

Received 31 January 2021

Received in revised form

3 June 2021

Accepted 23 June 2021

Available online 15 July 2021

### Keywords:

Membrane reactor

Computational fluid dynamics

Palladium (pd) membrane

## ABSTRACT

Methane steam reforming is the most widely used pathway for hydrogen production. In this context, the use of a fixed bed catalytic reactor with a hydrogen-selective membrane is one of the most promising technologies to produce high purity hydrogen gas. In this work, the membrane reactor three-dimensional computational fluid dynamic (CFD) model was developed to investigate the performance. In this model, methane steam reforming global kinetic model has been coupled with the CFD model using User-Defined Function (UDF). Whereas, hydrogen permeation across the membrane is implemented by introducing source and sink formulation. The CFD simulation results were compared to the experimental data, where the developed model successfully captured the experimentally observed trends. We studied the influence of the various operating parameters, as temperature, steam to carbon ratio, sweep gas flow configuration and space velocity on the

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<https://doi.org/10.1016/j.ijhydene.2021.06.178>

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Methane steam reforming  
Hydrogen separation

overall performance. The main observation and attained optimal operation windows from the study was discussed to provide insight into the factors affecting the overall performance.

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## Introduction

The industrial scale methane and other hydrocarbon fuel conversion to hydrogen ( $H_2$ ) is carried out by three main methods: steam reforming, partial oxidation, and auto-thermal reforming [1]. Among them methane steam reforming (MSR) has been accounting for approximately 48% of global  $H_2$  production [2–5]. Hydrogen-selective membranes have been employed in conventional packed bed reactors (PBR) and offer several advantages in terms of cost effectiveness and process efficiency [6–8]. The advantages include the increase in  $H_2$  production rate compared to that of a packed bed reactor at the same temperature. Moreover, membrane reactor (MR) can operate at milder conditions than conventional PBR. Another advantage of this hydrogen-selective membrane reactor is the conservation of additional  $H_2$  purification equipment cost. All these above-mentioned advantages stem due to Le Chatelier's principle.

The development of inorganic membranes has received attention because of their potential application for medium-high temperature operations. Particularly for the application of hydrogen gas separation several membranes have already been developed with various raw materials such as dense polymer, dense ceramic, dense metallic, porous carbon, mixed matrix membrane, etc. [9–13]. Among those, dense metallic-based membranes, especially Palladium (Pd) membranes, provide higher hydrogen perm-selectivity than those with other materials. Further, Palladium (Pd) membranes do not form an oxide layer unlike other dense membranes such as tantalum (Ta), niobium (Nb), and vanadium (V). Addition of alloying elements for example copper (Cu), yttrium (Y) and silver (Ag) help to improve  $H_2$  permeability and mechanical durability with no effect on selectivity. In literature, hollow fiber, flat-sheet, and tubular type metallic membranes were used for methane reforming process [6,14,15]. In membrane reactor, a pressure gradient is driving force for the hydrogen permeation. Essentially, high-pressure feed gas mixture is applied to the retentate side while maintaining low pressure on the permeate side. Higher hydrogen partial pressure seeds the permeation from high to low pressure.

Several researchers have studied the hydrogen separation utilizing a Pd-based membrane. Iulianelli et al. [16] perform the comparative experiment for MSR with and without Pd-MR at 450 °C and low pressures (1–3 bar). Observe methane conversion obtained in the PBR is 6% with respect to 50% obtained with the MR. Kim et al. [17] carried out MSR reaction at gas hourly space velocity (GHSV) = 1700  $h^{-1}$ , 773 K and steam to carbon ratio (S/C) = 3.0, for ~145 h in tubular Pd-based composite membrane reactor with a commercial Ru/ $Al_2O_3$  catalyst. Methane conversion increased at a higher transmembrane pressure difference, and reached 79.5% at a

transmembrane pressure difference of 507 kPa. Nayeboassadri et al. [18] studied hydrogen separation from blended natural gas and hydrogen using commercially available Pd, PdCu<sub>53</sub>, and PdAg<sub>24</sub> membranes. Separation capability was investigated under different hydrogen concentration, partial pressure, and temperature. Also, a possible interaction between gas impurity and membranes was investigated. Among these membranes, PdAg<sub>24</sub> effectively separated hydrogen concentrations as low as 15%. The use of Pd-based membranes requires large pressure gradient across the membrane surface and high temperatures (>350 °C) [19]. On the other hand,  $H_2$  rich gases containing CO affect  $H_2$  permeation performance [20]. All these factors make required to explore the qualitative behavior under different operating conditions.

As mentioned above, the experimental observations confirmed the advantageous feature of a membrane reactor including Pd-membranes. Currently, a variety of modeling tools have been utilized to predict reactor performances and facilitate the optimization of membrane reactors [21]. For example, modeling based on a one-dimensional (1-D) plug flow reactor is probably the simplest approach, but this method does not take into account comprehensive information pertaining to temperature, concentration, or velocity profiles [22,23]. Thus, more advanced simulation tools such as a multi-dimensional computational fluid dynamics (CFD) model should be provided to predict further realistic temporal and spatial distributions within membrane reactors. Benguerba et al. [24,25] developed a CFD model to study hydrogen separation through nickel/ $\alpha$ -alumina membrane. At low pressure, the performance of porous nickel membrane competed with the Pd–Ag membrane, but at higher pressure, nickel membrane selectivity weaken. Ghohe and Hormozi [26] numerically investigated the influence of geometrical shape on  $H_2$  separation over Pd-membrane using two-dimensional CFD model. Their study shows a higher average flux for conical shape compared to the cylindrical shape. Chen et al. [27] optimized multiple Pd membrane tube distribution to maximize the separation of  $CO_2$  and  $H_2$ . They showed that increase in the number of tubes raises the optimization efficiency. Optimized configuration at  $Re = 10$  the  $CO_2$  enrichment intensified by up to 7%, while hydrogen recovery up to 12.2%. Also, researchers paid attention to model chemical kinetics and separation phenomena in the single unit reactor [28]. Wei-Hsin Chen et al. [29] model hydrogen flux and concentration polarization in the palladium (Pd) membrane. In the membrane, source-sink terms following Sieverts' law were used in numerical study. Their numerical result show, higher hydrogen separation with counter-current flow compared to co-current flow configuration. Further, an increase in reactant feed rate with sweep gas influence the hydrogen permeation by increasing

the concentration polarization. Coroneo et al. [30] performed a CFD simulation for three different kinds of inorganic membrane modules. Their model introduced sink and source terms on the membrane boundary cells and shows good prediction against experimental data. Said et al. [31,32] simulated a molten salt-heated membrane reformer integrated into a parabolic trough solar facility. A 2D CFD model was developed to investigate and optimize the performance of a catalyst-assisted membrane-based reformer for hydrogen. Their operating temperature range was found to be suitable to make the reformer as the receiver of a parabolic trough solar collector. Sanusi et al. [33] simulated a membrane-based reformer–combustor reactor using CFD. Reforming, sweep, and combustion zone were simulated with 2-D axisymmetric domain. Firstly, methane steam reforming model was validated, and further membrane reactor was verified for different temperature. Their model study was firstly validated for methane steam reforming model then membrane reactor was further validated for different temperature sets. Xuan et al. [34] performed a numerical simulation of a microchannel reformer with a catalytic-supported membrane. In their study, a two-dimensional CFD model combined with chemical kinetics was developed with a key objective focusing on the modeling of local heat and mass transfer phenomena rather than whole system performance. Tahmasbi et al. [35] presented 2D axisymmetric CFD model of the silica membrane for  $H_2$  separation. On the tube zone species transfer was defined by source terms, whereas on the shell side transport of species was specified.

In spite of the many research accomplishments so far, all the above-mentioned simulation studies were mostly limited to the utilization of simplified 2D geometry or neglecting the steam reforming reaction in a reaction zone. Also, integration of the reaction kinetics and hydrogen separation were not considered within 3D geometry in previous models. In reality, it is desirable that both phenomena take place simultaneously should be incorporated in a multi-dimensional model. Furthermore, during long periods of operation, Pd-membrane permeance decline due CO adsorption on the membrane surface. Therefore, the present study primarily aimed to scan the membrane reactor performances over a wide range of space velocities, sweep gas flow reaction temperature including industrially relevant values. The outcomes of the CFD analysis are expected to be helpful for future design and optimization of the membrane modules for hydrogen separation.

### System description and operating condition

The membrane reactor geometry is created based on the experimental setup of Kim et al. [36]. Fig. 1 describes the three-dimensional membrane reactor geometry used in the simulation. The membrane reactor is composed of two domains: (a) reforming section (retentate domain) and (b) permeate domain separated by membrane layer. The computation domain has a length of 300 mm and a height of 25.4 mm. The membrane reactor was packed with commercial Ni/Al<sub>2</sub>O<sub>3</sub> catalyst and Pd–Ru membrane. In the retentate zone reforming reaction takes place, producing H<sub>2</sub>, CO<sub>2</sub>, and

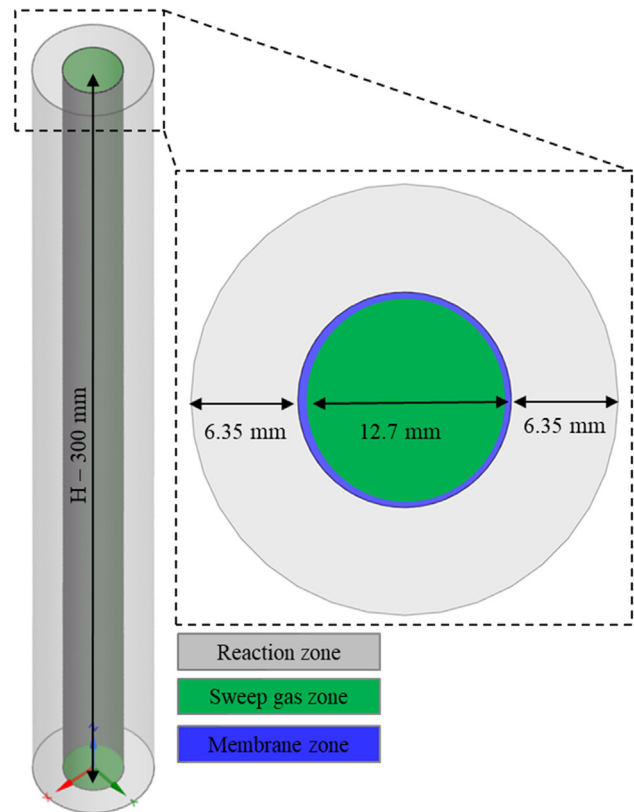


Fig. 1 – 3D membrane reactor computational domain.

CO species and leaves it from the outlet. As the gas species pass over membrane layer hydrogen is instantaneously permeated through the membrane to the permeate domain. In this work, we conceptually consider a permeate domain sweep gas from the bottom and top. The permeated hydrogen leaves the computation domain along with the sweeping gas from the top side of the permeation domain (permeate-outlet). In this work, both the retentate and permeate domain were included in the simulation. Other information on the simulation, such as the reactor geometry, and operating conditions are summarized in Table 1.

### Mathematical model

To accurately account the conversion of reactants (steam and methane) into products (hydrogen fuel) under different conditions, researcher coupled the reaction kinetics model with reactor-scale CFD modeling. Catalyst specific detail transport and reaction phenomena kinetic model incorporation is beyond the scope of this study. Therefore, catalyst bed was numerically simulated as porous media with volumetric species transport model. In the present study, widely-accepted simplified global kinetics expressions presented by Xu and Froment [37] are adopted. Tables 2 and 3 summarized the reaction rates with their corresponding kinetic, equilibrium, and adsorption constants. Apart from that, intraparticle diffusion limitations inside catalyst particles were incorporated by effectiveness factors for the reforming reactions [38,39]. For

**Table 1 – System geometry and operating conditions.**

Description	Value
Temperature, K	673–1273
Retentate pressure, kPa	200, 250
Permeate pressure, kPa	100
Gas hourly space velocity, h <sup>-1</sup>	837–10000
CH <sub>4</sub> : H <sub>2</sub> O	1:3
Length, mm	300
Membrane diameter, mm	12.7
Reactor diameter, mm	25.4

the reforming reactions, optimal effectiveness factors value were used.

For the MSR, a commercial spherical Ni/Al<sub>2</sub>O<sub>3</sub> (diameter of 1.5 mm) catalyst was used in this study. For Ni/Al<sub>2</sub>O<sub>3</sub> catalyst thermal conductivity of 33 W/m/K was used by Lao et al. [40]. For determining the composition, the mixture, mixing-law based on the species mass fraction was used. For calculating the density of mixture, volume-weighted-mixing-law was employed. The viscosity and thermal conductivity were estimated using the ideal-gas mixing law (or mass-weighted mixing law). In the present work, each gas component specific heat capacity (*c<sub>p</sub>*) were determined by a fourth-order polynomial and thermal conductivity (*λ<sub>i</sub>*) was estimated by the kinetic theory [41]. Whereas, the power law expression was used to estimate viscosity of each species.

To estimate the hydrogen permeation rate across the membrane, Sieverts' law-based equation has been widely accepted [42]. In the present numerical work, pair of source and sink terms were implemented in the species transport equation. The overall permeation was calculated by multiplying Sievert's law with a parameter *A<sub>c</sub>/V<sub>c</sub>*, where *A<sub>c</sub>* is cell area and *V<sub>c</sub>* is the cell volume, as shown by eq. (4)

$$\phi = \beta \cdot M_{w,H_2} \frac{A_c P_e}{V_c l} \exp\left(-\frac{E_a}{RT}\right) \left(p_{r,H_2}^{0.5} - p_{p,H_2}^{0.5}\right) \quad (4)$$

## Results and discussion

### Mesh sensitivity analysis

To determine the optimal number of grid cells to achieve both model accuracy and efficiency in simulation, various sets of the cell numbers were applied in a preliminary model

**Table 3 – The MSR reaction constants.**

Kinetic constant coefficients:	$k_1 = 4.22 \times 10^{15} \exp\left(-\frac{240,100}{RT}\right)$
	$k_2 = 1.96 \times 10^6 \exp\left(-\frac{67,130}{RT}\right)$
	$k_3 = 1.02 \times 10^{15} \exp\left(-\frac{243,900}{RT}\right)$
Equilibrium constants:	$K_{e1} = 1.198 \times 10^{13} \exp\left(-\frac{26,830}{RT}\right)$
	$K_{e2} = 1.767 \times 10^{-2} \exp\left(\frac{4,400}{RT}\right)$
	$K_{e3} = 2.117 \times 10^{11} \exp\left(-\frac{22,430}{RT}\right)$
Adsorption constants:	$K_{CH_4} = 6.65 \times 10^{-4} \exp\left(\frac{38,280}{RT}\right)$
	$K_{H_2O} = 1.77 \times 10^5 \exp\left(-\frac{88,680}{RT}\right)$
	$K_{H_2} = 6.12 \times 10^{-9} \exp\left(\frac{82,900}{RT}\right)$
	$K_{CO} = 8.23 \times 10^{-5} \exp\left(\frac{70,650}{RT}\right)$

test. ANSYS meshing tool was used to discretized the 3D domain into hexahedral grid. Four different grid cell sizes of 2, 1, 0.75, and 0.5 mm were used, for which about 20400, 156300, 362400, and 1253400 number of grid were constructed respectively in order to investigate the effect of grid size (see Fig. 2). Methane conversion was selected as the judging variable to determine whether the model solution needs further refinement. As shown in Fig. 3, a higher methane conversion value was obtained with very course grid, but methane conversion value decreased and finally showed similar conversion for the grid containing up to 156300 mesh numbers. Thus, the grid was not refined further to save the computational time.

### Membrane reactor model validation

Before investigating the key operating parameter, the developed MSR kinetic model was verified by operating the retentate domain identical to temperature, pressure, and space velocity of Xu and Froment [37]. The operation condition includes the reaction temperature of 848 K at the pressure of 10 bar with a steam-to-methane (S/C) ratio equal to 3. As a result of the validity test, Fig. 4 (a) depicts the simulated data, compared with their corresponding experimental methane conversion data reported by Xu and Froment [37].

Further, the developed Sieverts' law-based hydrogen permeation model was verified against the experimental data

**Table 2 – Methane steam reforming (MSR) reaction rates.**

Steam reforming reaction (SR): CH <sub>4</sub> + H <sub>2</sub> O => 3H <sub>2</sub> + CO	$r_1 = \frac{k_1(P_{CH_4}P_{H_2O} - P_{H_2}^3P_{CO}K_{e1}^{-1})}{P_{H_2}^{2.5}DEN^2}$
Water gas shift reaction (WGSR): CO + H <sub>2</sub> O => H <sub>2</sub> + CO <sub>2</sub>	$r_2 = \frac{k_2(P_{CO}P_{H_2O} - P_{H_2}P_{CO_2}K_{e2}^{-1})}{P_{H_2}DEN^2}$
Direct steam reforming reaction (DSR): CH <sub>4</sub> + 2H <sub>2</sub> O => 4H <sub>2</sub> + CO <sub>2</sub>	$r_3 = \frac{k_3(P_{CH_4}P_{H_2O}^2 - P_{H_2}^4P_{CO_2}K_{e3}^{-1})}{P_{H_2}^{3.5}DEN^2}$
	$DEN = 1 + K_{CO}P_{CO} + K_{H_2}P_{H_2} + K_{CH_4}P_{CH_4} + K_{H_2O} \left(\frac{P_{H_2O}}{P_{H_2}}\right)$

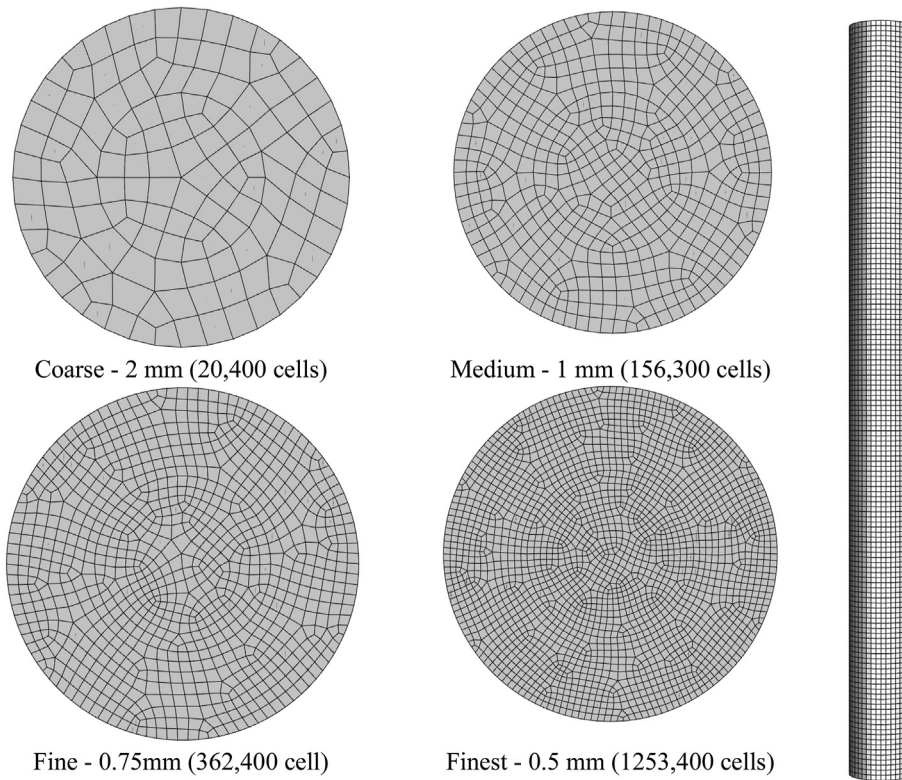


Fig. 2 – Membrane reactor grid resolution in the computational domain.

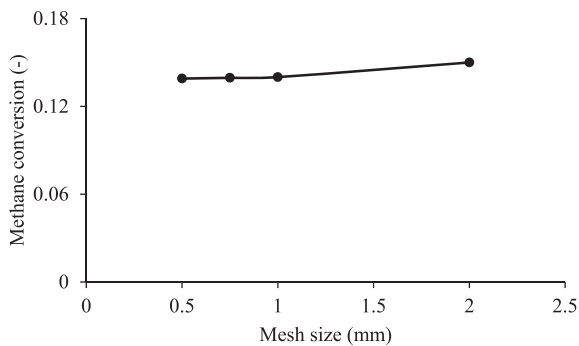


Fig. 3 – The simulated methane conversions for different grid resolutions.

reported by Kim et al. [36]. Initially, MSR kinetic model was run at the same operating condition, after achieving a pseudo steady state hydrogen permeation model initiated. Model prediction for two different operating pressure shows the same methane conversion as we observed in the experiment, as shown in Fig. 4b. The resultant comparison between numerical and experimental results revealed the ability of the CFD to successfully predict the experiment data.

#### Effects of reaction temperature

The reaction temperature is a key parameter in the membrane reactor, and therefore the estimation of the performance of the reactor for different temperatures should be important for

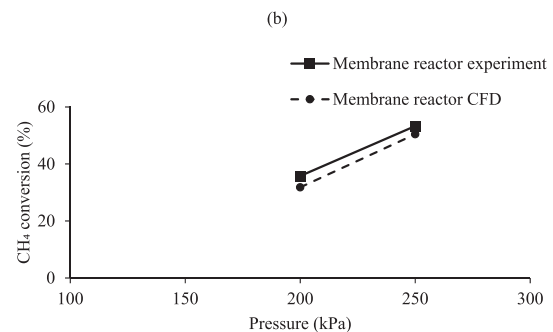
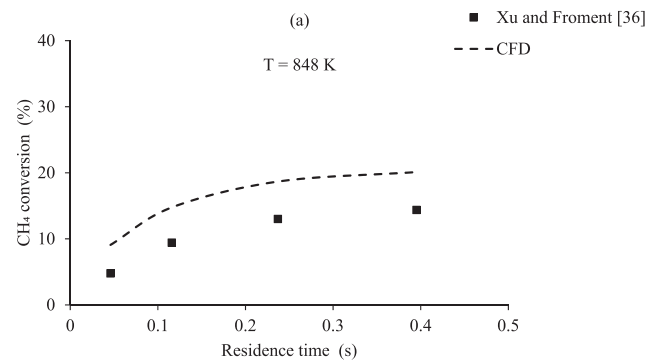
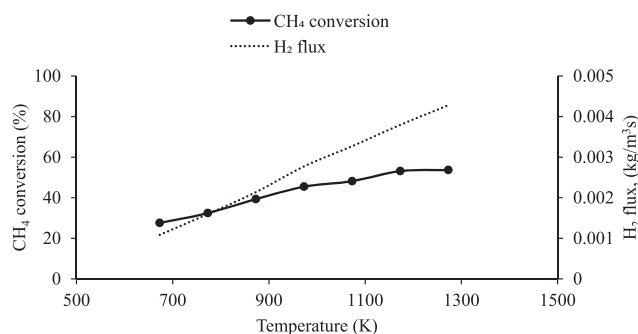


Fig. 4 – (a) MSR model validation at T – 848 K, P – 1000 kPa, S/C – 3 (b) Membrane reactor model validation at T – 773 K; GHSV – 837 h<sup>-1</sup>; S/C – 3; P – 200, 250 kPa.



**Fig. 5 – Effect of reaction temperature on methane conversion and hydrogen flux through the membrane. (GHSV – 837 h<sup>-1</sup>; S/C – 3; P – 200 kPa).**

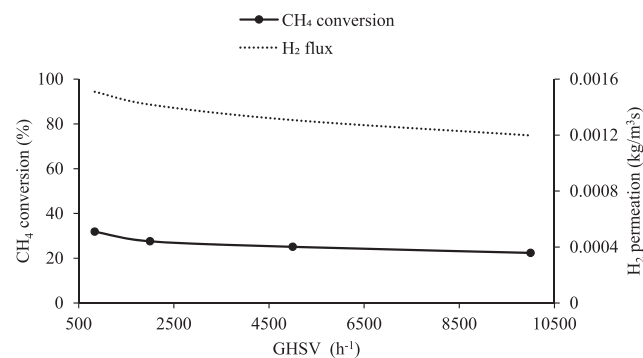
practical application. To analyze the influence of reaction temperature, the simulation was performed under fixed GHSV of 837 h<sup>-1</sup>, S/C ratio of 3 and retentate pressure of 200 kPa. The temperature was varied in the range of 673–1273 K. As shown in Fig. 5, methane conversion as a function of the temperature is constantly increased due to the endothermic characteristic as previously shown in the literature [43]. Along with methane conversion, hydrogen permeation rate as a function of temperature was plotted in Fig. 5. As the operating temperature increases the hydrogen separation rate is promoted Eq. (4). These predictions are in accordance with previous findings from literature [33,44].

For facilitating qualitative understanding, the model results of all three products (hydrogen, carbon dioxide, and carbon mono-oxide) obtained from the CFD simulation are visualized in Fig. 6. It seems that the CFD simulation was successfully able to capture the experimental trend of hydrogen, carbon dioxide, and carbon monoxide concentration as observed in the experiment [36]. Also, the hydrogen and carbon dioxide species concentration clearly increased with increasing in temperature. Indeed, the highest hydrogen species can be achieved by increasing the reforming temperature, because the steam reforming reaction is endothermic, favoring the high reaction temperatures. The quantitative comparison exhibited the obvious increase of the mean hydrogen mass fraction value with an increase in the reaction

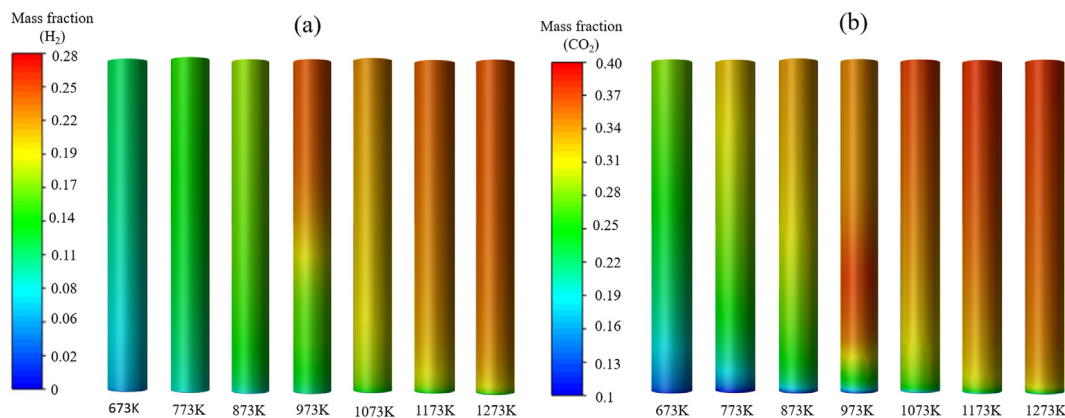
temperature. Overall performance of membrane reactor monotonically increases with temperature. However, the rate of methane conversion from 673 K to 973 K highest compared to temperature range of 1073 K–1273 K. Therefore, considering the Pd inorganic membrane performance with thermal stability the recommended operating temperature conditions between 673 K and 973 K.

### Effect of GHSV

Another key operating parameter, the gas hourly space velocity (GHSV) was utilized to quantify the residence time of the reactant gases in a reactor during the operation. To find the potential application towards a large scale operation, the performance of MR was explored over a large range of GHSV. Fig. 7 shows the model results on the methane conversion according to the change of GHSV ranging from 837 h<sup>-1</sup> to 10,000 h<sup>-1</sup>, at the operating temperature and pressure of 773 K and 200 kPa respectively. From the modeling, with the given GHSV ranges, it seems that the methane conversion slightly decreased with an increase in GHSV. These predictions are consistent with other researcher findings [45]. However, increasing GHSV led to lower methane conversion, CH<sub>4</sub> conversion of 22% was still achievable by the membrane reformer. At higher GHSV



**Fig. 7 – Effect of GHSV on methane conversion and hydrogen flux through the membrane. (GHSV – 837 h<sup>-1</sup>; S/C – 3; P – 200 kPa).**



**Fig. 6 – Contour plot of (a) H<sub>2</sub> species, (b) CO<sub>2</sub> species for different reaction temperature (GHSV – 837 h<sup>-1</sup>; S/C – 3; P – 200 kPa).**

result into decreasing the contact time with the membrane surface, which cause more decrease in  $H_2$  permeation rate through the membrane as shown in Fig. 7. Similar observation was reported by Ma et al. [45]. However, in the meantime, a higher amount of  $CH_4$  was feed into a reactor with higher GHSV. Thus, a very high feed rate of  $CH_4$  gives reduction in the overall conversion rate.

In Fig. 8, it can be seen that at lower GHSV, a higher contact time in the reaction domain was favored. Specially, at low GHSV, helps higher hydrogen formation rate in the downstream direction. Thus, favor the higher hydrogen partial pressure which enhances the  $H_2$  permeation and  $CO_2$  adsorption rate helps effective shifting toward the products yield. Fig. 8b shows the temperature distribution profile for different GHSV (837, 2000, 5000, and 10000  $h^{-1}$ ). Here, the counterplot shows the temperature profile on the ZX plane. The simulation result shows two distinctive temperature profiles for retentate and permeate zone. The contour profile clearly explains that the mean temperature value is highest for 837  $h^{-1}$  GHSV operating condition and lowest for 10000  $h^{-1}$  GHSV operating condition. The above results highlight that for higher GHSV value methane conversion reached a plateau, thus considering the amount of reactant feed into membrane reactor require further detail parameter study in future work.

### Effect of steam to carbon (S/C) ratio

After the analysis of the gas hourly space velocity, the reactant feed flow rate was fixed at a GHSV of 837  $h^{-1}$ . Methane steam reforming in membrane reactor was tested under different steam to carbon ratio (S/C). Steam to methane (S/C) feed molar ratio is one of the key operational parameters that has large influence [46]. To understand the effect on the  $CH_4$  conversion at the various steam-to-methane ratio simulation were carried out under fixed GHSV of 837  $h^{-1}$ , 1073 k and retentate pressure of 200 kPa. The steam to methane ratio was varied in the range of 1–4. According to the Le Chatelier's principle, an increase in the reactant concentrations favored the forward reaction direction, therefore increase the methane conversion. Accordingly, the methane conversion increased from 45% to 49% for

the corresponding increase in S/C ratios from 1 to 3, as shown in Fig. 9. The CFD model prediction shows good agreement with other published results [47,48]. However, in the presence of an excess of steam in the feed stream (S/C = 4), gives lower methane conversion, similar phenomenon has been previously observed in the literature [47]. Fig. 9 also reports hydrogen permeation rate for varying steam to methane ratio. As seen, the clear improvements achieved for hydrogen permeation as S/C increases from 1 to 3, whereas hydrogen permeation drops at S/C = 4. This outcome indicates that the excess steam diluted the mixture concentration and decreased hydrogen partial pressure difference between the reaction and the permeation zones [46]. The simulation results show that the influence of S/C ratio on the methane conversion and hydrogen permeation, it can be seen that the S/C of 3 is the optimal value.

### Effect of sweep gas flow pattern

The membrane reactor performance in terms of methane conversion and hydrogen permeation for two different sweep flow configurations, namely co-current and counter-current was investigated. We evaluated the performance over range of sweep gas flow rate to attain optimum condition. By increasing the sweep gas flow rate  $CH_4$  conversion and  $H_2$

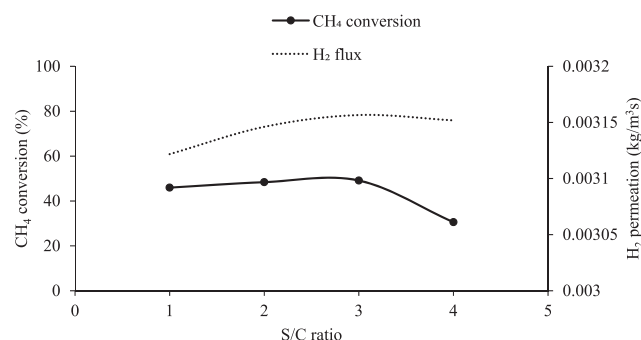


Fig. 9 – Effect of steam to carbon ratio on methane conversion and hydrogen flux through the membrane. (GHSV – 837  $h^{-1}$ ; P – 200 kPa).

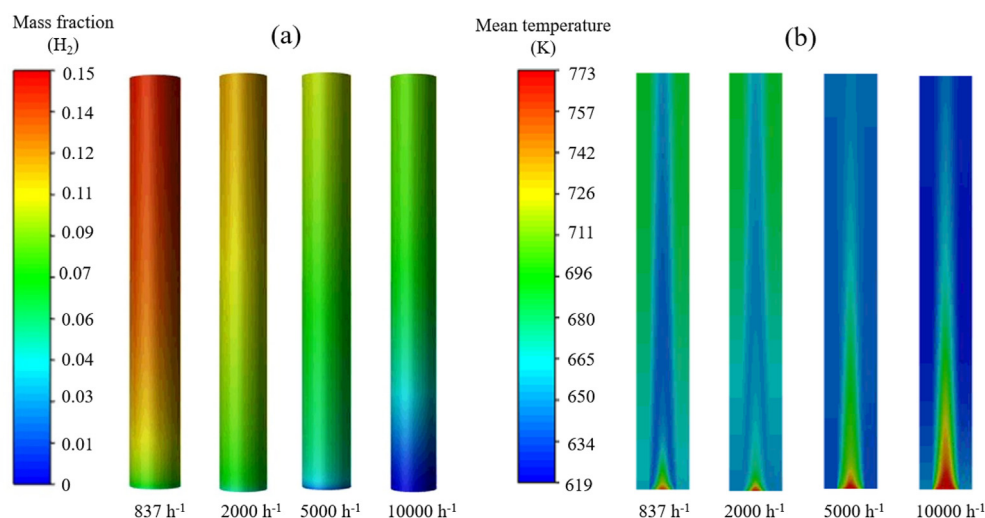
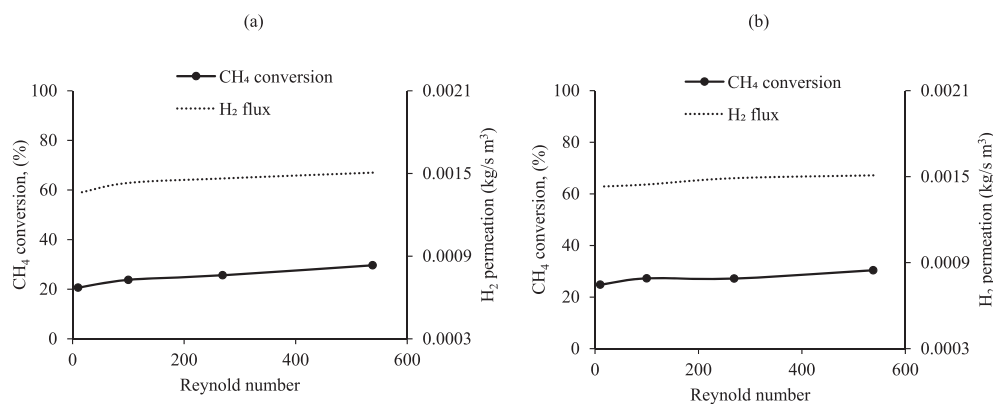


Fig. 8 – Contour plot of (a)  $H_2$  species, (b) Z-X plan temperature profile for different GHSV (S/C – 3; P – 200 kPa).



**Fig. 10** – Effect of (a) co-current (b) counter current, sweep flow configuration on methane conversion and hydrogen flux through the membrane. (GHSV – 837 h<sup>-1</sup>; S/C – 3; P – 200 kPa).

permeation increases for both counter-current and co-current mode as exhibited in Fig. 10. In particular, for the constant reactant feed rate, when the sweep gas flow rates increased, the average H<sub>2</sub> permeation across the membrane in co-current and counter-current flow configuration was enhanced by 7.8 and 12.6%, respectively. Similar increased permeation rate phenomenon was reported by Abdi et al. [49] and Gallucci et al. [50]. This implied that the sweep gas was able to effectively increase the H<sub>2</sub> permeation rate. As for the effect of the flow direction, H<sub>2</sub> separation from the counter-current mode was found to be better than that from the co-current once, this trend was consistent with the observations in the other studies [29]. Therefore, it is also found that H<sub>2</sub> separation positive influences resulting increased methane conversion with counter-current mode of operation. Increasing the flow rate of sweep gas diminished the difference of average H<sub>2</sub> permeation between the two current configurations. In particular, once the flow rate of sweep gas was higher, the difference became smaller. Such phenomena due to lessened concentration polarization on the membrane surface for a higher sweep gas flow rate. Overall performance between two flow configurations becomes smaller for a higher sweep gas flow rate. Such results clearly prove that continuous removal of hydrogen on the permeate zone enhances the overall hydrogen permeation. A sweep flow configuration sensitivity analysis suggest that counter-current modes give better performance in the whole range sweep gas flow rate. It is important to notice that at low sweep gas flow rate the methane conversion is high.

## Conclusion

In the proposed study, the performance of a Palladium (Pd) membrane reactor for methane steam reforming (MSR) was demonstrated through a comprehensive three-dimensional (3D) computational fluid dynamic (CFD) analysis. For this purpose, retentate zone reforming reaction incorporate using the Xu and Forment kinetic model and hydrogen permeation via source and sink terms. Prior to detail operating sensitivity

analysis, MSR reaction kinetic and permeation model were successfully validated with experimental data.

The developed model was then applied to investigate various operating conditions of the membrane reactor, and the results can be summarized as follows:

- 1) Simulation result proved that operating temperature is one of most influencing operation parameters. Temperature range of 673 K–973 K revealed optimal for balancing permeation and reaction performance.
- 2) Reduction in overall residence time resulted from an increase in the gas flow rate, leading to a decrease in H<sub>2</sub> permeation. Hence, methane conversion and H<sub>2</sub> separation performances higher at lower GHSV.
- 3) With increasing the steam to methane (S/C) ratios from 1 to 3, methane conversion increased from 45% to 49%, except for the ratio of 4.
- 4) Simulation results predicts increase in the CH<sub>4</sub> conversion and H<sub>2</sub> permeation with increase in sweep gas flow rate. Also, we observe that the permeation and reaction performance with counter-current configuration is better than the co-current configuration.

## Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

## Acknowledgement

This work was supported by the Korea Institute of Energy Technology Evaluation and Planning (KETEP) granted financial resource from the Ministry of Trade, Industry & Energy, Republic of Korea (No. 20183010032380) also this research was supported by the Hydrogen Energy Innovation Technology Development Program of the National Research Foundation of

Korea funded by the Korean government (Ministry of Science and ICT (MSIT)) (NRF-2019M3E6A1064290).

## Appendix A

### Continuity equation and Momentum conservation equation

Continuity equation:

$$\nabla \cdot (\rho \vec{u}) = 0 \quad (a)$$

Momentum equation:

$$\nabla \cdot (\rho \vec{u} \vec{u}) = -\nabla p + \nabla \cdot \vec{\tau} + \rho g + F \quad (b)$$

$$F = -\left(\frac{\mu_e \vec{u}}{\alpha} + C_0 \frac{1}{2} \rho |\vec{u}| \vec{u}\right), \mu_e = \mu(1 + 2.5(1 - \gamma))$$

Energy Equation:

$$\nabla \cdot (\vec{u}(\rho E + p)) = \nabla \cdot \left( k_{\text{eff}} \nabla T + \sum h_i \overline{j_i} + (\vec{u} \cdot \vec{\tau}_{\text{eff}}) \right) + \sum h_i R_i + \nabla \cdot \vec{q}_{\text{rad}} \quad (c)$$

Species equation:

$$\nabla \cdot (\rho \vec{u} Y_i) = \nabla \cdot \vec{j}_i + R_i \quad (d)$$

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## Nomenclature

T: Temperature (K or °C)

P: Pressure (kPa)

$p_i$ : Partial pressure of species i, bar

D: Diameter, mm

L: Length, mm

$r_n$ : nth chemical reaction rate (kmol/m<sup>3</sup>/s)

$k_n$ : Kinetic parameter of reaction nth (Table 3)

$K_{eq}$ : Equilibrium constant (Table 3)

$K_i$ : Adsorption constants of species i (Table 3)

R: Gas constant ( $8.314 \times 10^3$  J/kmol/K)

$c_p$ : Specific heat capacity (J/kg/K)

$M_w$ : Molecular weight (kg/kmol)

$A_c$ : Area of membrane boundary cell (m<sup>2</sup>)

$V_c$ : Volume of membrane boundary cell (m<sup>3</sup>)

$P_e$ : Pre-exponential factor (mol/m<sup>2</sup>s/Pa<sup>0.5</sup>)

l: Membrane thicknesses (m)

$P_{r,H_2}$ : Partial pressure of hydrogen in retentate side (Pa)

$P_{p,H_2}$ : Partial pressure of hydrogen in permeate side (Pa)

$E_a$ : Activation energy (kJ/mol)

## Greek Letters

$\gamma$ : Thermal conductivity (W/m/K)

$\mu_i$ : Viscosity of the ith species (kg/m/s)

$\beta$ : Membrane effectiveness factor (–)

## Abbreviation

GHSV: Gas hourly space velocity

CFD: Computational fluid dynamics